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## ON TWO QUESTIONS OF NICHOLSON

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ABSTRACT. We show that a ring R has stable range one if and only if every left unit lifts modulo every left principal ideal. We also show that a left quasi-morphic ring has stable range one if and only if it is left uniquely generated. Thus we answer in the affirmative the two questions raised by W. K. Nicholson.

Mathematics Subject Classification (2020): 16U60, 16D50

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